

What is a ratio?

A ratio is a comparison between two numbers. Ratios are used to compare two different things.

For example: a bowl may contain two kinds of fruit, 9 pieces of fruit in total, made up of five apples and four oranges. Suppose you want to express the ratio of apples to oranges in the bowl of fruit. Then the ratio of apples to oranges is 5 to 4, and can be written as: 5:4.



Ratio Practice

Try these out ...

- Q1. Given that there is 100g of butter and 500g of flour in a cake, what would be the ratio of butter to flour?
- Q2. If there are 9 students doing chemistry and 11 students doing English, what is the ratio of chemistry to English students?

Ratio Practice Answers
Q1. 100:500, which simplifies to 1:5.
Q2. 9:11, which cannot be further simplified.

How Ratios are Written

Remember a ratio is a comparison between two numbers. There are many different ways of writing a ratio but ratios are often written with a colon (:).

For example: 1:2, $\frac{1}{2}$, 1 out of 2, 1 is to 2, 0.5 and 50% are all ways of writing the ratio 1:2 and they are all equal. ($1:2 = \frac{1}{2} = 1:2 = 1 \text{ is to } 2 = 0.5 = 50\%$)

Be careful with units!

1 litre: 2 millilitre = 1000mL: 2mL = 500:1 (NB not a ratio of $\frac{1}{2}$ or 1:2)

A proportion is a statement that two ratios are equal

For example: $1:2 = 2:4 = 3:6$
 $\frac{2}{5} = \frac{4}{10}$

Ratio and Proportion Sample Questions

- Q3. Determine if the ratio 2:3 is equal to the ratio 8:11.
- Q4. You want to make up a 400mL mixture made up of 25% of solution A and 75% of solution B. How many mL of A do you need?
- Q5. 20% of your population is blue-eyed. If you have 3450 people in your population, how many of them have blue eyes?
- Q6. There are some books on the shelf and 12 are cookbooks. If 20% are cookbooks, how many books are on the shelf?
- Q7. A cordial drink is to be made up using 30% cordial concentrate and 70% water. If a jug holds 1000 mL, how many mLs of water will need to be added to the cordial concentrate to make up one litre of cordial drink?
- Q8. The recipe for strawberry jam says 3.5kg of sugar for 4kg of strawberries. I have only 3kg of strawberries. How much sugar do I need?

Ratio and Proportion Worked Solutions to Sample Questions

Q3. Determine if the ratio 2:3 is equal to the ratio 8:11.

To work it out, firstly write the ratio as a proportion: $\frac{2}{3} = \frac{8}{11}$

Then you can either:

(a) remember that for fractions to be equal, you must be able to multiply top and bottom numbers by the same amount, which does **not** work in this case:

Multiplying the first fraction by the same number on both top and bottom of the fraction, and not getting the numbers in the second fraction, tells us these two fractions are not equal.

$$\frac{2}{3} = \frac{8}{11}$$

$2 \times 4 = 8$
 $3 \times 4 \neq 11$ ✗

$$\frac{2}{3} = \frac{8}{12}$$

$2 \times 4 = 8$
 $3 \times 4 = 12$ ✓

(b) replace one of the numbers with a ? and use cross-multiplication to work out that the ratios are not equal:

$$\frac{2}{3} = \frac{?}{11}$$

Multiply along the orange line: $2 \times 11 = 22$

Divide along the second orange line: $22/3 = 7.33$ (approx.)

Since 7.33 is not equal to 8, you know the ratios are not equal.

Q4. You want to make up a 400mL mixture made up of 25% of solution A and 75% of solution B. How many mL of A do you need?

The total mixture is 400mL and the number of mLs of A is what we don't know and want to find.

25% of A and 75% of B means that $\frac{1}{4}$ of the mixture will be A and $\frac{3}{4}$ will be B.

Since we want to find the number of mLs of A, we use the ratio $\frac{1}{4}$.

Multiplying by the same number on both top and bottom of the fraction keeps the fraction the same.

$$\frac{1}{4} = \frac{?}{400}$$

$1 \times 100 = 100$
 $4 \times 100 = 400$

The answer is that we need 100mL of solution A.

Q5. 20% of your population is blue-eyed. If you have 3450 people in your population, how many of them have blue eyes?

The total population is 3450 and we want to know how many of them have blue eyes. If 20% are blue-eyed, this means that $\frac{20}{100} = \frac{1}{5}$ of the population is blue-eyed. We write our equation this way:

Multiplying by the same number on both top and bottom of the fraction keeps the fraction the same.

$$\frac{1}{5} = \frac{?}{3450}$$

$1 \times 690 = 690$
 $5 \times 690 = 3450$

The answer is that 690 people are blue-eyed.

Q6. There are some books on the shelf and 12 are cookbooks. If 40% are cookbooks, how many books are on the shelf?

There are 12 cookbooks and the total number of books is what we want to know. If 40% are cookbooks, this means that $\frac{40}{100} = \frac{2}{5}$ of the books are cookbooks. We write our equation this way:

Multiplying by the same number on both top and bottom of the fraction keeps the fraction the same.

$$\frac{2}{5} = \frac{12}{?}$$

$2 \times 6 = 12$
 $5 \times 6 = 30$

The answer is that there is a total of 30 books on the shelf.

Q7. A cordial drink is to be made up using 30% cordial concentrate and 70% water. If a jug holds 700 mL, how many mLs of water will need to be added to the cordial concentrate to make up one litre of cordial drink?

The total mixture is 700mL and the number of mLs of water is what we want to find out. 30% of concentrate and 70% of water means that $\frac{70}{100} = \frac{7}{10}$ of the mixture will be concentrate and $\frac{30}{100} = \frac{3}{10}$ of the mixture will be water.

Since we want to find the number of mLs of water, we use the ratio 7/10.

Multiplying by the same number on both top and bottom of the fraction keeps the fraction the same.

$$\frac{7}{10} = \frac{?}{700}$$

$7 \times 70 = 490$
 $10 \times 70 = 700$

The answer is that we need 490mL of water.

Q8. The recipe for strawberry jam says 3.5kg of sugar for 4kg of strawberries. I have only 3kg of strawberries. How much sugar do I need?

I need 3.5kg sugar and 4kg strawberries, which makes the ratio 3.5: 4 or the fraction $\frac{3.5}{4}$. But, since I only have 3kg strawberries, I want to know how much sugar will keep the proportion of sugar to jam the same. I can write this as follows: $3.5 \times \frac{3}{4} = 2.625$

Multiplying by the same number on both top and bottom of the fraction keeps the fraction the same.

$$\frac{3.5}{4} = \frac{?}{3}$$

$$4 \times \frac{3}{4} = 3$$

The answer is that we need 2.625kg of sugar.

This time, it's trickier to see what to multiply 4 by in order to get 3. If it is too hard to see, you can always use the cross-multiply method below.

Finding Ratio Amounts – STEPS

1. Write the ratios out vertically.
2. Make sure there are three numbers present and one unknown letter variable.
3. Cross multiply the items.
4. Divide both sides by the number which is in front of the letter variable.
5. Write the simplified answer.

Ratio Amounts – Example One

$a : 15 = 2 : 5$ Find the value of "a"

$$\begin{array}{l} 2 : 5 \\ a : 15 \end{array}$$

Write the ratios out vertically, and then Cross Multiply

$$2 \times 15 = 5 \times a \quad (\text{Note writing } 2 \times 15 = a \times 5 \text{ is also okay})$$

$$30 = 5a$$

"5" is the number in front of the letter variable and so divide both sides of the equals sign by 5 and simplify.

$$\frac{30}{5} = \frac{5a}{5}$$

$$6 = a \Rightarrow a = 6 \quad \checkmark$$

Ratio Amounts – Example Two

$4 : 11 = 80 : k$ Find the value of "k"

$$\begin{array}{l} 4 : 11 \\ 80 : k \end{array}$$

Write the ratios out vertically, and then Cross Multiply

$$4 \times k = 11 \times 80 \quad (\text{Note writing } k \times 4 = 80 \times 11 \text{ is also okay})$$

$$4k = 880$$

"4" is the number in front of the letter variable and so divide both sides of the equals sign by 4 and simplify.

$$\frac{4k}{4} = \frac{880}{4}$$

$$k = 220 \quad \checkmark$$

STUDENT LEARNING CENTRE
REGISTRY BUILDING ANNEXE

TEL: 61-8-8201 2518
E-MAIL: slc@flinders.edu.au

INTERNET: <http://www.flinders.edu.au/SLC>
POSTAL: PO Box 2100, ADELAIDE, SA 5001